

**McGill University**  
**ECN 706**  
**Special topics in econometrics**  
**Mid-term exam**

No documentation allowed  
Time allowed: 1.5 hour

- 30 points
1. Provide brief answers to the following questions (maximum of 1 page per question).
    - (a) Explain the difference between the “level” of a test and its “size”.
    - (b) Explain the difference between the “level” of a confidence set and its “size”.
    - (c) Discuss the link between tests and confidence sets: how confidence sets can be derived from tests, and vice-versa.

- 40 points
2. Consider the following simplified equilibrium model:

$$\begin{aligned}D_t &= \alpha + 2p_t + u_{1t}, \\S_t &= c + u_{2t}, \\Q_t &= D_t = S_t \quad , t = 1, \dots, T\end{aligned}$$

where  $D_t$  is the demand for a product,  $S_t$  the supply for the same product, and  $Q_t$  the quantity produced and sold. We suppose that the vectors  $(u_{1t}, u_{2t})'$ ,  $t = 1, \dots, T$ , are independent and  $N[0, I_2]$ .

- (a) Find the reduced form of this model.
- (b) For which parameters is the vector  $Q = (Q_1, \dots, Q_T)'$  exogenous? Justify your answer.
- (c) For which parameters is the vector  $p = (p_1, \dots, p_T)'$  exogenous? Justify your answer.
- (d) Are the variables  $Q_t$  and  $p_t$  simultaneous?

30 points 3. Consider the linear regression model

$$y = X\beta + u \quad (0.1)$$

where  $y$  is a  $T \times 1$  vector of observations on a dependent variable,  $X$  is a  $T \times k$  fixed matrix of explanatory variables (observed),  $\beta = (\beta_1, \dots, \beta_k)'$ , and  $u = (u_1, \dots, u_T)'$  is a  $T \times 1$  vector of unobserved error terms. Suppose the elements of  $u$  are independent and identically distributed according to a  $\sigma t(1)$  distribution, where  $t(1)$  represents a Student  $t$  distribution with 1 degree of freedom and  $\sigma$  is an unknown constant.

- (a) Propose a method for testing the hypothesis  $H_0 : \beta_1 = 1$  at level  $\alpha = 0.05$  in the context of this model such the size of the test is exactly equal to  $\alpha = 0.05$ .
- (b) Propose a test for detecting serial dependence between the errors  $u_1, \dots, u_T$  such the size of the test is exactly equal to  $\alpha = 0.05$ .