

Jean-Marie Dufour
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McGill University
ECN 706
Special topics in econometrics
Final exam

No documentation allowed
Time allowed: 3 hours

- 20 points 1. Provide brief answers to the following questions (maximum of 1 page per question).
- (a) Explain the difference between the “level” of a test and its “size”.
 - (b) Explain the difference between the “level” of a confidence set and its “size”.
 - (c) Discuss the link between tests and confidence sets: how confidence sets can be derived from tests, and vice-versa.
 - (d) Explain what the Bahadur-Savage theorem entails for testing in nonparametric models.
 - (e) Suppose we wish to test the hypothesis

$$H_0 : X_1, \dots, X_n \text{ are independent random variables} \quad (1)$$

each with a distribution symmetric about zero.

What condition should this test satisfy to have level 0.05.

- 20 points 2. State and prove the *Neyman-Pearson theorem*.
- 10 points 3. Explain how invariant tests can reduce the number of nuisance parameters in a test problem.
- 30 points 4. Consider the standard simultaneous equations model:

$$y = Y\beta + X_1\gamma + u, \quad (2)$$

$$Y = X_1\Pi_1 + X_2\Pi_2 + V, \quad (3)$$

where y and Y are $T \times 1$ and $T \times G$ matrices of endogenous variables, X_1 and X_2 are $T \times k_1$ and $T \times k_2$ matrices of exogenous variables, β and γ are $G \times 1$ and $k_1 \times 1$ vectors of unknown coefficients, Π_1 and Π_2 are $k_1 \times G$ and $k_2 \times G$ matrices of unknown coefficients, $u = (u_1, \dots, u_T)'$ is a $T \times 1$ vector of structural disturbances, and $V = [V_1, \dots, V_T]'$ is a $T \times G$ matrix of reduced-form disturbances,

$$X = [X_1, X_2] \text{ is a full-column rank } T \times k \text{ matrix} \quad (4)$$

where $k = k_1 + k_2$. and

$$u \text{ and } X \text{ are independent;} \quad (5)$$

$$u \sim N[0, \sigma_u^2 I_T]. \quad (6)$$

- (a) When is the parameter β identified? Explain your answer.
- (b) When is the parameter β weakly identified? Explain your answer.
- (c) Suppose we wish to test the hypothesis

$$H_0(\beta_0) : \beta = \beta_0. \quad (7)$$

- i. Describe the standard Wald-type test for $H_0(\beta_0)$ based on two-stage-least-squares, and describe its properties.
- ii. Describe an identification-robust procedure for testing $H_0(\beta_0)$.
- iii. Discuss the properties of the latter procedure if the model for Y is in fact

$$Y = X_1\Pi_1 + X_2\Pi_2 + X_3\Pi_3 + V \quad (8)$$

where X_3 is a $T \times k_3$ matrix of fixed explanatory variables.

20 points 5. Discuss the relationships between the following concepts:

- (a) Granger causality and prediction;
- (b) Granger causality and causality at several horizons;
- (c) Granger causality and impulse response coefficients;
- (d) causality at several horizons and impulse response coefficients.